

INTEGRAL ESTIMATION IN QUANTUM PHYSICS

by

Jane Doe

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in
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The University of Utah Graduate School

STATEMENT OF DISSERTATION APPROVAL

The dissertation of Jane Doe
has been approved by the following supervisory committee members:

<u>Cornelius Lánczos</u> ,	Chair(s)	<u>17 Feb 2016</u>
		Date Approved
<u>Hans Bethe</u> ,	Member	<u>17 Feb 2016</u>
		Date Approved
<u>Niels Bohr</u> ,	Member	<u>17 Feb 2016</u>
		Date Approved
<u>Max Born</u> ,	Member	<u>17 Feb 2016</u>
		Date Approved
<u>Paul A. M. Dirac</u> ,	Member	<u>17 Feb 2016</u>
		Date Approved

by Petrus Marcus Aurelius Featherstone-Hough, Chair/Dean of
the Department/College/School of Mathematics
and by Alice B. Toklas, Dean of The Graduate School.

For my parents, Alice and Bob.

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NOTATION AND SYMBOLS

α	fine-structure (dimensionless) constant, approximately 1/137
α	radiation of doubly-ionized helium ions, He++
β	radiation of electrons
γ	radiation of very high frequency, beyond that of X rays
γ	Euler's constant, approximately 0.577 215 ...
δ	stepsize in numerical integration
$\delta(x)$	Dirac's famous function
ϵ	a tiny number, usually in the context of a limit to zero
$\zeta(x)$	the famous Riemann zeta function
...	...
$\psi(x)$	logarithmic derivative of the gamma function
ω	frequency

TYPESETTING EXPERIMENTS

In this section, we use color in several places. The `\colorbox` command takes two arguments — a named color and text to be in black on a background of that color — and sets the text in a box with a small margin of width `\fboxsep` (set to 3.0pt in this document).

Here, we want a tighter colored box that has a fixed height, and is independent of letter shape. We set the margin to zero inside a group so that the change is purely local, and so that height and depth of the line are not increased over what they would be if the colored box were not used. We prefix a TeX `\strut` to the user-supplied text, because that command expands to a zero-width box of the height and depth of parentheses, which, in most fonts, delimit the extent of letter shapes.

```
\newcommand {\hilitebox} [1] {{\fboxsep = 0pt\colorbox{pink}{\strut #1}}}
```

Here is a fragment from the first chapter in another thesis, set in *emphasized text* to distinguish it from the rest of this section:

In light of the known results, the consistency of empirical semivariogram and related estimators is widely considered a settled matter. For example, Lahiri, Lee, and Cressie [22] state:

The simpler and more commonly used nonparametric estimators of the variogram, such as the method of moments estimator of Matheron (1962) and its robustified versions due to Cressie and Hawkins (1980) have many desirable properties like, unbiasedness, consistency, etc. . . .

Regarding a kernel estimator of the covariance function, Hall and Patil [14] remarked:

It is not difficult to see that if, as n increases, the points t_i become increasingly dense in each bounded subset of \mathbb{R}^d , then the bandwidth h may be chosen so that $\check{\rho}(t) \rightarrow \rho(t)$ as $n \rightarrow \infty$, for each $t \in \mathbb{R}^d$.

However, in order to be true, such statements would need to be qualified by many assumptions on the random field as well as on the observation locations. We will see in §2.3 that even for well-behaved random fields (e.g., ρ^ -mixing Gaussian random fields), it is not enough to assume that the observation locations become increasingly dense in each bounded subset; a stronger assumption*

must be made to ensure that the observation locations do not become denser in one region too much faster than in others.

The text before the previous paragraph contained two quote environments separated by a line of prose. Here are some more tests of both kinds of L^AT_EX environments for showing text written by someone else.

This is a **quote** environment with one short line, following a fairly short paragraph of prose (in this, and following examples, the text is explicitly colored with a command like `\color{purple}` inside the environment before the text):

```
\begin{quote}
  \color{purple}
  14 March 2016 is $\\pi \\approx 3.1416$ day in funny notation.
  \\hfill \\emph{Web news reports}
\end{quote}
```

14 March 2016 is $\pi \approx 3.1416$ day in funny notation. *Web news reports*

This is a **quote** environment with three short lines, each a separate paragraph, following a fairly short paragraph of prose.

```
\begin{quote}
  \color{forestgreen}
  14 March 2016 is $\\pi \\approx 3.1416$ day in funny notation.
  \\hfill \\emph{Web news reports}

  14 March 2016 is $\\pi \\approx 3.1416$ day in funny notation.
  \\hfill \\emph{Web news reports}

  14 March 2016 is $\\pi \\approx 3.1416$ day in funny notation.
  \\hfill \\emph{Web news reports}
\end{quote}
```

14 March 2016 is $\pi \approx 3.1416$ day in funny notation. *Web news reports*

14 March 2016 is $\pi \approx 3.1416$ day in funny notation. *Web news reports*

14 March 2016 is $\pi \approx 3.1416$ day in funny notation. *Web news reports*

Here is another example, this time with separate colors for each paragraph:

```
\begin{quote}
```

```

\color{darkkhaki}
14 March 2016 is $\pi \approx 3.1416$ day in funny notation.
\hfill \emph{Web news reports}

\color{darkmagenta}
14 March 2016 is $\pi \approx 3.1416$ day in funny notation.
\hfill \emph{Web news reports}

\color{darkcyan}
14 March 2016 is $\pi \approx 3.1416$ day in funny notation.
\hfill \emph{Web news reports}

\color{darkorange}
14 March 2016 is $\pi \approx 3.1416$ day in funny notation.
14 March 2016 is $\pi \approx 3.1416$ day in funny notation.
14 March 2016 is $\pi \approx 3.1416$ day in funny notation.
\linebreak
\strut
\hfill \emph{Web news reports}
\end{quote}

```

14 March 2016 is $\pi \approx 3.1416$ day in funny notation. *Web news reports*

14 March 2016 is $\pi \approx 3.1416$ day in funny notation. *Web news reports*

14 March 2016 is $\pi \approx 3.1416$ day in funny notation. *Web news reports*

14 March 2016 is $\pi \approx 3.1416$ day in funny notation. 14 March 2016 is $\pi \approx 3.1416$ day in funny notation. 14 March 2016 is $\pi \approx 3.1416$ day in funny notation. *Web news reports*

Web news reports

Notice that `quote` paragraphs are *not* indented, but the environment itself *is* indented on the left and right by the value of `\leftmargin` (set to 27.37506pt in this document, which should be identical to `2.5em`, where `1em` = 11.49739pt).

For debugging purposes, we also have `\leftmargini` set to 27.37506pt, and we have `\leftmarginii` set to 24.09003pt.

This is a `quotation` environment with one paragraph, following a fairly short paragraph of prose (notice that the quotation paragraphs *are* indented):

```

\begin{quotation}
\color{blue}
Algebra is concerned with manipulation in
\emph{time}, and geometry is concerned with
\emph{space}. These are two orthogonal aspects
of the world, and they represent two different

```

points of view in mathematics. Thus the argument or dialogue between mathematicians in the past about the relative importance of geometry and algebra represents something very fundamental.

\hfill

```
\emph{Sir Michael Atiyah}
% Mathematics in the 20$^{th}$ century
% NTM {\bf 10}(1--3) 25--39 (September 2002)
% http://dx.doi.org/10.1007/BF03033096
\end{quotation}
```

Definitions

Algebra is concerned with manipulation in *time*, and geometry is concerned with *space*. These are two orthogonal aspects of the world, and they represent two different points of view in mathematics. Thus the argument or dialogue between mathematicians in the past about the relative importance of geometry and algebra represents something very fundamental. *Sir Michael Atiyah*

This is a **quotation** environment with three paragraphs, following a fairly short paragraph of prose:

Algebra is concerned with manipulation in *time*, and geometry is concerned with *space*. These are two orthogonal aspects of the world, and they represent two different points of view in mathematics. Thus the argument or dialogue between mathematicians in the past about the relative importance of geometry and algebra represents something very fundamental. *Sir Michael Atiyah*

Algebra is concerned with manipulation in *time*, and geometry is concerned with *space*. These are two orthogonal aspects of the world, and they represent two different points of view in mathematics. Thus the argument or dialogue between mathematicians in the past about the relative importance of geometry and algebra represents something very fundamental. *Sir Michael Atiyah*

Algebra is concerned with manipulation in *time*, and geometry is concerned with *space*. These are two orthogonal aspects of the world, and they represent two different points of view in mathematics. Thus the argument or dialogue between mathematicians in the past about the relative importance of geometry and algebra represents something very fundamental. *Sir Michael Atiyah*

and on and on and on

Chapter 1

THE FIRST

This is a chapter. Remember that there should *always* be at least of few lines of prose after each sectional heading: failure to do so is a disservice to your readers, and also produces incorrect vertical spacing.

1.1 The first section

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah blah.

In [Figure 1.1](#) on page 8, we have a picture, and the `LATEX` markup to include it looks like this:

```
\begin{figure}[p]
  \centerline{\includegraphics{fig1}}
  \caption{The first figure.}%
  \figlabel{fig1}
\end{figure}
```

We intentionally omitted an extension on the filename, so that this document can be processed with `latex` to get an output `.dvi` file, or with `pdflatex` to get an output `.pdf` file. The first case uses the file `fig1.eps`, and the second uses `fig1.pdf`. The `distill` or `ps2pdf` commands can be used to convert from *Encapsulated PostScript* files to *Portable Document Format* files.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah.

1.1.1 The first subsection

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah blah.

1.1.2 The second subsection

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah.

1.1.3 The third subsection

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah.

1.1.3.1 The first subsubsection

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah.

1.1.3.2 The second subsubsection

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah.

1.1.3.2.1 The first numbered paragraph Blah blah blah blah blah blah
blah blah blah blah blah blah. Blah blah blah blah blah blah blah
blah blah blah blah blah. Blah blah blah blah blah blah blah blah
blah blah blah blah.

1.1.3.2.2 The second numbered paragraph Blah blah blah blah blah blah
blah blah blah blah blah blah. Blah blah blah blah blah blah
blah blah blah blah blah. Blah blah blah blah blah blah blah
blah blah blah blah.

1.2 The second section

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah.

In [Table 1.1](#) on the next page, we show the 24-character lowercase Greek alphabet.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah.

Blah blah blah blah blah blah blah blah blah blah.
Blah blah blah blah blah blah blah blah blah blah. Blah
blah blah blah blah blah blah blah blah.

In [Figure 1.2](#) on page 8, we have another picture.

Blah blah blah blah blah blah blah blah blah blah.
Blah blah blah blah blah blah blah blah blah blah. Blah
blah blah blah blah blah blah blah blah.

Blah blah blah blah blah blah blah blah blah blah.

Table 1.1. Lowercase Greek letters.

α	alpha
β	beta
γ	gamma
δ	delta
ϵ, ε	epsilon
ζ	zeta
η	eta
θ, ϑ	theta
ι	iota
κ	kappa
λ	lambda
μ	mu
ν	nu
ξ	xi
\circ	omicron
π	pi
ρ	rho
σ, ς	sigma
τ	tau
v	upsilon
ϕ, φ	phi
χ	chi
ψ	psi
ω	omega

1.3 The third section

Blah blah.
 Blah blah. Blah
 blah blah blah blah blah blah blah blah blah blah blah blah blah blah.

In **Table 1.2** on the next page, we show the 24-character uppercase Greek alphabet, 13 of which are identical with Latin letters, because the Romans borrowed several letters from the earlier Greek alphabet. However, the letter sounds do not always carry over: notice in particular the different names of the letter shapes **H** and **P**. In Modern Greek, β is pronounced *veeta*; the letter pair *υπ* is used to get a *bee* sound;

Blah blah.
 Blah blah. Blah
 blah blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
 Blah blah. Blah
 blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
 Blah blah. Blah
 blah blah blah blah blah blah blah blah blah blah.

Blah blah.
 Blah blah. Blah
 blah blah blah blah blah blah blah blah.

1.4 Free software packages

The Free Software Foundation offers almost 300 software packages, most easily portable to many different operating systems and CPU platforms. They include at least these:

```
a2ps, acct, acm, adns, alive, anubis, apl, archimedes, aris, aspell, auctex,
autoconf-archive, autoconf, autogen, automake, avl, ballandpaddle, barcode, bash,
bayonne, bc, binutils, bison, bool, bpel2owfn, c-graph, ccaudio, ccd2cue, ccrtcp,
ccscript, cfengine, cflow, cgicc, chess, cim, classpath, classpathx, clisp, combine,
commoncpp, complexity, config, coreutils, cpio, cppi, cssc, cursynth, dap, datamash,
ddd, ddrescue, dejagnu, denemo, dico, diction, diffutils, dionysus, direvent,
```

Table 1.2. Uppercase Greek letters. Notice that several have the same letter shapes as Latin letters, and for those, TeX does not define macro names. For convenience, we supply our own definitions of these macros: \Alpha, \Beta, \Epsilon, \Zeta, \Eta, \Iota, \Kappa, \Mu, \Nu, \Omicron, \Rho, \Tau, and \Chi.

A	Alpha
B	Beta
Γ	Gamma
Δ	Delta
E	Epsilon
Z	Zeta
H	Eta
Θ	Theta
I	Iota
K	Kappa
Λ	Lambda
M	Mu
N	Nu
Ξ	Xi
O	Omicron
Π	Pi
P	Rho
Σ	Sigma
T	Tau
Y	Upsilon
Φ	Phi
X	Chi
Ψ	Psi
Ω	Omega

```
dismal, dominion, easejs, ed, edma, electric, emacs, emms, enscript, fdisk, ferret,
findutils, fisicalab, flex, fontutils, freedink, freefont, freeipmi, gama, garpd,
gawk, gcal, gcc, gcide, gcl, gcompris, gdb, gdbm, gengen, gengetopt, gettext,
gforth, ggradebook, ghostscript, gift, gleem, glibc, global, glpk, gmp, gnash,
gnats, gnatsweb, gnu-c-manual, gnu-crypto, gnu-pw-mgr, gnubatch, gnubik, gnucap,
gnucobol, gnudos, gnue, gnugo, gnuuit, gnujump, gnukart, gnumach, gnuun, gnunet, gnupod,
gnuprologjava, gnuradio, gnurobots, gnuschool, gnushogi, gnusound, gnuspeech,
gnuspool, gnustep, gnutls, gnutrition, gnuzilla, goptical, gperf, gprolog, greg,
grep, groff, grub, gsasl, gsgrafix, gsl, gslip, gsrc, gss, gtypist, guile-gnome,
guile-gtk, guile-ncurses, guile-opengl, guile-rpc, guile-sdl, guile, gv, gvpe,
```

```
gxmessage, gzip, halifax, health, hello, help2man, hp2xx, http tunnel, hurd, hyperbole,
idutils, ignuit, indent, inetutils, intlfonts, jacal, jel, jwhois, kawa, less,
libcdio, libextractor, libffcall, libiconv, libidn, libmatheval, libmicrohttpd,
librejs, libsigsegv, libtasn1, libtool, libunistring, libxmi, lightning, lilypond,
liquidwar6, lsh, m4, macchanger, mailman, mailutils, make, marst, maverik, mc, mcron,
mcsim, mdk, metahtml, mifluz, mig, miscfiles, mit-scheme, moe, motti, mpc, mpfr,
mpria, mtools, myserver, nano, ncurses, nettle, non-gnu, ocrad, octave, oleo, orgadoc,
osip, paperclips, parallel, parted, patch, pem, pexec, phantom, pies, plotutils,
proxyknife, pspp, psychosynth, pth, pyconfigure, radius, rcs, readline, recutils,
reftex, remotecontrol, rottlog, rpge, rush, sather, sauce, savannah, scm, screen,
sed, serveez, sharutils, shishi, shmm, shtool, sipwitch, slib, smalltalk, solfege,
spacechart, spell, sqltutor, src-highlight, stow, superopt, swbis, tar, termcap,
termutils, teseq, teximpatient, texinfo, thales, time, tramp, trueprint, unifont,
units, unrtf, userv, uucp, vc-dwim, vcdimager, vera, wb, wdiff, websocket4j, wget,
which, windows, xaos, xboard, xhippo, xlogmaster, xnee, xorriso, and zile.
```

Blah blah.
 Blah blah. Blah
 blah blah blah blah blah blah blah blah blah blah blah blah blah blah blah.

In [Figure 1.3](#) on the following page, we have yet another picture.

Blah blah.
 Blah blah. Blah
 blah blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
 Blah blah. Blah
 blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
 Blah blah. Blah
 blah blah blah blah blah blah blah blah blah blah.

Blah blah.
 Blah blah. Blah
 blah blah blah blah blah blah blah blah blah.



Figure 1.1. The first figure.



Figure 1.2. The second figure.



Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah.

Blah blah blah blah blah blah blah blah blah blah.
Blah blah blah blah blah blah blah blah blah blah. Blah
blah blah blah blah blah blah.

Blah blah blah blah blah blah blah blah blah blah.
Blah blah blah blah blah blah blah blah blah blah. Blah
blah blah blah blah blah.

Blah blah blah blah blah blah blah blah blah.
Blah blah blah blah blah blah blah blah blah. Blah
blah blah blah blah blah.

1.5 Resizing figures

In [Figure 1.4](#) on page 11 through [Figure 1.8](#) on page 11, we show how graphics files can be rescaled to convenient sizes.

```
\begin{figure}[p]
  \centerline{\includegraphics[scale = 0.5]{fig1}}
  \caption{The fourth figure (at 50\% scale).}%
```

```
\figlabel{fig4}
\end{figure}

\begin{figure}[p]
\centerline{\includegraphics[scale = 0.75]{fig1}}
\caption{The fifth figure (at 75\% scale).}%
\figlabel{fig5}
\end{figure}

\begin{figure}[p]
\centerline{\includegraphics{fig1}}
\caption{The sixth figure (at native size).}%
\figlabel{fig6}
\end{figure}

\begin{figure}[p]
\centerline{\includegraphics[scale = 1.25]{fig1}}
\caption{The seventh figure (at 125\% scale).}%
\figlabel{fig7}
\end{figure}

\begin{figure}[p]
\centerline{\includegraphics[scale = 1.75]{fig1}}
\caption{The eighth figure (at 175\% scale).}%
\figlabel{fig8}
\end{figure}
```

You can include multiple images, each with its own caption inside a single *unbreakable* figure environment, like this example shown in [Figure 1.9](#) and [Figure 1.10](#).

```

\begin{figure}[b]
    \centerline{\includegraphics[scale = 0.5]{fig1}}
    \caption{The fourth figure (at 50\% scale).}%
    \figlabel{fig9}
\end{figure}

\begin{figure}[b]
    \centerline{\includegraphics[scale = 0.75]{fig1}}
    \caption{The fifth figure (at 75\% scale).}%
    \figlabel{fig10}
\end{figure}

```



This is Figure 1

Figure 1.4. The fourth figure (at 50% scale).



This is Figure 1

Figure 1.5. The fifth figure (at 75% scale).



This is Figure 1

Figure 1.6. The sixth figure (at native size).



This is Figure 1

Figure 1.7. The seventh figure (at 125% scale).



This is Figure 1

Figure 1.8. The eighth figure (at 175% scale).

blah blah.

Blah blah.
 Blah blah. Blah
 blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
 Blah blah. Blah
 blah blah blah blah blah blah blah blah blah blah blah.

As a final example in this chapter, [Figure 1.11](#) on the next page shows how you can use \LaTeX picture mode for annotating and positioning graphics images prepared outside \LaTeX . The input that produced that figure looks like this:

```
\begin{figure}[b]
  %% The original image is 216bp wide by 72bp high, but we
  %% rescale it to 150 picture units divided by \unitlength:
  %% 150 / 0.75 = 112.5 mm
  \newcommand {\myfig} {\includegraphics[width = 112.5mm]{fig1}}

  \begin{center}
    %% The \unitlength is chosen to make the complete picture fit
    %% within the page margins

    \setlength{\unitlength}{0.75mm}

    %%      insert (width,height)(lower-left-x,lower-left-y)
    \begin{picture}(170,70)(10,10)
      %% Place the included image FIRST!
      \put(10,10) {\myfig}
    \end{picture}
  \end{center}

```

This is Figure 1

[Figure 1.9](#). The ninth figure (at 50% scale), boxed with the tenth figure.

This is Figure 1

[Figure 1.10](#). The tenth figure (at 75% scale), boxed with the ninth figure.

```

%% Everything that follows OVERLAYS the original image!

\graphpaper[10](0,0)(170,70)

%% Mark the image center and corners by centered bullets
\newcommand{\thedadot}{\makebox(0,0){$.\bullet$}}
\put( 85, 35){\thedadot}
\put( 10, 10){\thedadot}
\put( 10, 60){\thedadot}
\put(160, 10){\thedadot}
\put(160, 60){\thedadot}

\put( 10, 10){\makebox(0,0)[r]{lower-left}}
\put(160, 10){\makebox(0,0)[l]{lower-right}}
\put( 10, 60){\makebox(0,0)[r]{upper-left}}
\put(160, 60){\makebox(0,0)[l]{upper-right}}
\end{picture}
\end{center}

\vspace{2\baselineskip}

\caption[Using \LaTeX{} \texttt{picture} mode]
{Using \LaTeX{} \texttt{picture} mode for figure labeling and positioning.}
\figlabel{picture-mode}
\end{figure}

```

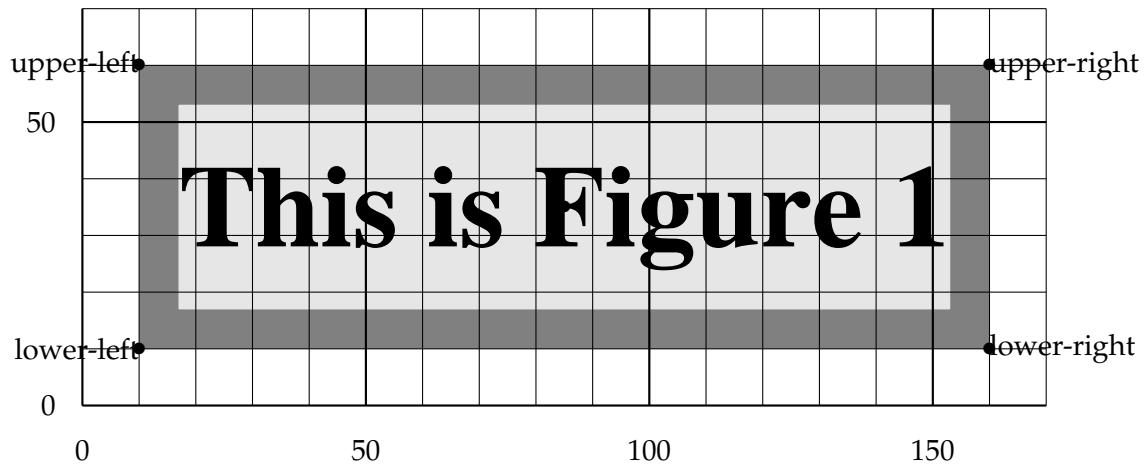


Figure 1.11. Using \LaTeX picture mode for figure labeling and positioning.

1.6 Summary and conclusions

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah blah. Blah blah
blah blah blah blah blah blah blah blah blah blah blah blah blah blah. Blah blah blah
blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah.

Chapter 2

THE SECOND

This is a chapter.

Blah blah.

Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah blah.

Chapter 3

THE THIRD

This is a chapter.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah blah.

Chapter 4

THE FOURTH

This is a chapter.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah blah.

Blah blah.
Blah blah. Blah
blah blah blah blah blah blah blah blah blah blah blah blah blah.

4.1 More on the topic

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4.2 Even more on the topic

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4.3 Summary and conclusions

Blah blah. Blah blah. Blah blah.

Appendix A

THE FIRST

This is an appendix. Notice that the L^AT_EX markup for an appendix is, surprisingly, `\chapter`. The `\appendix` command does not produce a heading; instead, it just changes the numbering style from numeric to alphabetic, and it changes the heading prefix from **CHAPTER** to **APPENDIX**.

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Appendix B

THE SECOND

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Appendix C

THE THIRD

This is an appendix.

There are several books [12, 19–21, 23–25, 27–30] listed in our bibliography.

We also reference several journal articles [1, 2, 4, 8–10, 13–18, 22, 31, 32] and three famous doctoral theses of later winners [3, 6, 7] of the Nobel Prize in Physics (1922, 1933, and 1921):

Notice that, even though those citations appeared in `\cite{...}` commands with their BIBTEX citation labels in reverse alphabetical order, thanks to the `citesort` package, their reference-list numbers have been sorted in numerically ascending order, and then range-reduced.

Mention should also be made of this famous computer scientist's first publication [5].

Font metrics are an important, albeit low-level, aspect of typesetting. See the *Adobe Systems* manual about that company's procedures [26].

The world's first significant computer program may have been that written in 1842 by Lady Augusta Ada Lovelace (1815–1852) for the computation of Bernoulli numbers [16, 18]. She was the assistant to Charles Babbage (1791–1871), and they are the world's first computer programmers. The programming language *Ada* is named after her, and is defined in the ANSI/MIL-STD-1815A Standard; its number commemorates the year of her birth.

We do not discuss mathematical *transforms* in this dissertation, but you can find that phrase in the index.

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